to others. Number Operations in Base Ten Progressions document P ()

ssential Question(s):	Common Preconceptions/Misconceptions:
 What are efficient methods for finding products and quotients? How are the different methods related? How do you determine which strategy you want to use? How does the context of a problem situation determine how to represent a remainder in division? How are operations with decimals similar to or different from operations used with whole numbers? How is estimation used to check the reasonableness of the computation involved in solving a problem? What strategies can be developed to estimate and compute products and quotients of numbers expressed as decimals? 	-Students believe they must use "the standard traditional algorithm" when any algorithm that makes sense to them and always leads to a correct response is not only acceptable and many times preferred if it is based on place value instead of just memorizing a procedure. -Students confuse rules for lining up decimals for adding and subtracting with rules for multiplication and division, especially when there is a lack of understanding with what the decimals represent and the place value. -Students confuse expected size of products and quotients for decimals with whole numbers: -When multiplying whole numbers the product is larger, but when multiplying by a decimal less than one the product gets smaller; Likewise when dividing whole numbers the quotient aets smaller, but

In real life, we use whole numbers and decimal computation every day. We need to be able to determine when it is appropriate to use mental math, paper and pencil or a calculator and use methods that make sense to ourselves and

FCPS 2023 - 2024 Math Unit 2 Framework

CRA explanations for 5th grade Unit 2 Big Idea(s)

Unit 2 Multiplying and Dividing Whole Numbers and Decimals, Convert in Metric

Unit 2 Title: Multiplying and Dividing Whole Numbers and Decimals, Convert in Metric

Essential Standards: 5.NBT.2, 5.NBT.5, 5.NBT.6, 5.NBT.7, Supporting Standards: 5.MD.1

Unit 2 framework google link

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KY 5th grade Math Standards

Estimated Time Frame: 47 days

5th grade Math Priority Content & Prerequisite Skills

	when dividing by a decim larger. <u>The Problem with Ke</u>	nal less than one the quotient gets y Words
Standards for Mathematical Practice (bolded practices are emphasized in this unit) <u>Math Practice Standards Posters</u>	Kentucky Interdisciplinary	v Literacy Practices (KILP)
 MP.1. Make sense of problems and persevere in solving them. MP.2. Reason abstractly and quantitatively. MP.3. Construct viable arguments and critique the reasoning of others. MP.4. Model with mathematics. MP.5. Use appropriate tools strategically. MP.6. Attend to precision. MP.7. Look for and make use of structure. MP.8. Look for and express regularity in repeated reasoning. 	 Recognize that text is any message. Employ, develop, and ref create text. View literacy experiences and transformational. Utilize receptive and expr understand self, others, and Apply strategic practices independently, to approach Collaborate with others to Utilize digital resources to Engage in specialized, di Apply high level cognitive critically about text. Develop a literacy identi 	Athing that communicates a ine schema to understand and is as transactional, interdisciplinary ressive language arts to better the world. , with scaffolding and then new literacy tasks. o create new meaning. learn and share with others. scipline specific literacy practices. e processes to think deeply and ty that promotes lifelong learning.
Essential Standards: KAS Content Standards <u>CRA explanations for 5th grade Unit 2</u>	Prerequisite Skills & Essential Vocabulary	Sample Learning Intentions* & Sample Success Criteria*
 KY.5.NBT.2 Multiply and divide by powers of 10. Explain patterns in the number of zeros of the product when multiplying a number by powers of 10. 	exponent power	I am learning to explain the movement of the decimal when multiplying or dividing by powers

 Explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10. MP.3, MP.8 	base	of ten so I can write numbers using exponents.
 Students recognize when a number is multiplied by 10, a zero is added to the end because each digit's value became 10 times larger. Students use the same reasoning to explain in the problem. 523 × 10³ = 523,000 The place value of 523 is increased by 3 places. 5.223 × 10² = 522.3 The place value of 5.223 is increased by 2 places. 52.3 ÷ 10¹ = 5.23 The place value of 52.3 is decreased by one place. Note: grade 5 expectations in this domain are limited to decimals through the thousandths place. Coherence KY.5.NBT.2→ KY.6.EE.1 		
KY.5.NBT.5 Fluently multiply multi-digit whole numbers (not to exceed four-digit by two-digit multiplication) using an algorithm. MP.7, MP.8 Students make connections from previous work with multiplication, using models/representations to develop an efficient algorithm to multiply multi-digit whole numbers.	-Multiply whole numbers: -Up to four digit number by a one-digit number -Two-digit number by two-digit number Multiply using strategies based on place value and the properties of	 I am learning to use visual models and equations to multiply whole numbers so I can represent multiplication with base-10 blocks and with place value strategies such as partial products.

Grade: 5

FCPS 2023 - 2024 Math Unit 2 Framework

Unit 1 Unit 2 Unit 3 Unit 4

1 300 70 4 × 53 50 15,000 3,500 200 =18,700 12 (3 × 4) 3 900 210 12 =1,122 900 (3 × 300) 900 (3 × 300) 19,822 200 (50 × 4) 3,500 (50 × 70) 15,000 (50 × 300) 19,822 15,000 (50 × 300) 19,822 Coherence KY.4.NBT.5→ KY.5.NBT.5→KY.6.NS.3	operations. Illustrate and explain the calculation by using equations, rectangular arrays and/or area models. product factors partial products efficient algorithm	 I can use models and representations to solve problems with multiplication.
 KY.5.NBT.6 Divide up to four-digit dividends by two-digit divisors. a. Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors using strategies based on place value the properties of operations the relationship between multiplication and division b. Illustrate and explain the calculation by using equations, rectangular arrays and/or area models. MP.2, MP.3, MP.4 Students build upon the knowledge of division they gained in grades 3 and 4. Students connect previous understanding of partitive and measurement models for division to an algorithm, including partial quotients. Some examples include: 968 ÷ 21 = Students use base ten models by representing 962 and use the model to make an array with one dimension of 21. Students continue to 	-Divide up to four-digit dividends by one-digit divisors. Find whole number quotients and remainders using: -strategies based on place value -the properties of operations -the relationship between multiplication and division Illustrate and explain the calculation by using equations, rectangular arrays and/or area models.	 I am learning to use visual models and equations to divide whole numbers so I can represent and explain division with base-10 blocks, area models, and with place value strategies such as partial quotients. I can use models and representations to solve problems with division.

make arrays until no more groups of 21 can be made. Remainders are not part of the array.	dividend	
	divisor	
	quotient	
	partial quotients	
Students use an area model for division shown below. As		
much of the 9,984 is left to divide.		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		
Students use expanded notation $2682 \div 25 = (2000 + 600)$		
relationship between 100 and 25, to think "I know 100		
divided by 25 is 4 so 200 divided by 25 is 8 and 2000		
Since 3 × 25 is 75, I know that 80 divided by 25 is 3 with a		
remainder of 5. I can't divide 2 by 25 so 2 plus the 5		
107 with a remainder of 7." Students use an equation that		
relates division to multiplication, 25 × n = 2682, a student		

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might estimate the answer to be slightly larger than 100 because s/he recognizes that $25 \times 100 = 2500$. Coherence KY.4.NBT.6 \rightarrow KY.5.NBT.6 \rightarrow KY.6.NS.2		
KY.5.NBT.7 Operations with decimals to hundredths.a. Add, subtract, multiply and divide decimals to hundredths using• concrete models or drawings• strategies based on place value• properties of operations• the relationship between addition and subtractionb. Relate the strategy to a written method and explain the reasoning used. MP.2, MP.3, MP.5Students connect previous experiences with the meaning of multiplication and division of whole numbers to multiplication and division of decimals using estimation, models and place value structure. For example: 3 tenths subtracted from 4 wholes. The wholes must be divided into tenthsThe answer is 3 and $\frac{7}{10}$ or 3.7Students describe the partial products displayed by the area model. For example,	-Fluently multiply and divide multi-digit whole numbers. Decimal	I am learning to use visual models and equations to add, subtract, multiply, and divide decimals so I can represent decimal operations: addition, subtraction, multiplication and division with base-10 blocks or grids. I am learning to add, subtract, multiply, and divide decimals to the hundredths place so I can use place value strategies, estimation, and properties of operations with decimals to solve problems.



that makes sense for the values in the problem. For example, for 1234×12 , they see the small numbers lend to a break apart strategy and solve the problem this way: $1234 \times 10 = 12340 \ 1234 \times 2 = 2468$ Then add the partial products to equal

14,808 (MP.7). Other students may stack the two values and use an algorithm. Students recognize a rectangle is an effective model for ensuring all partial products are calculated, for both whole numbers and decimals (MP.4). As students explore problems with decimal values, they reason about the problem, rather than following rules devoid of meaning (count the number of decimal places). For example, when multiplying 4×1.5 , they use a break apart strategy, as they have for whole numbers, noticing $4 \times 1 = 4$ and $4 \times 0.5 = 2$, so therefore, $4 \times 1.5 = 6$ (MP.2). They explain why this works and when they use this strategy (MP.3).

Supporting Standards:

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KY.5.MD.1 Convert among different size measurement units (mass, weight, liquid volume, length, time) within one system of units (metric system, U.S. standard system and time) (in later unit)*. MP.3, MP.8	-Know relative size of measurement units (mass, weight, liquid volume, length, time) within one system of	I am learning to relate decimal place value to converting in metric units in solving multi- step real world problems so • I can convert metric units
Within the same system convert measurements in a larger unit in terms of a smaller unit and a smaller unit in terms of a larger unit. Use these conversions in solving multi-step, real world problems. Coherence KY.4.MD.1→ KY.5.MD.1→KY.6.RP.3	units (metric system, U.S. standard system and time). a. Understand the relationship of measurement units within any given	of length. I can convert metric units of capacity. I can convert metric units of mass.
*(U.S. standard system and time will be in a later unit.)	measurement system. b. Within any given measurement system, express measurements in a larger unit in terms of a smaller unit. c. Record measurement equivalents in a two-column table.	

Attending to the Standards for Mathematical Practice

Students notice patterns about how units and measurements relate to each other (MP.8). For example, students measure various objects in meters and in centimeters (using a meter stick). As they measure their items, they record the measurements in a table. They notice the object that measures about 300 centimeters also measures about 3 meters (MP.8). They explain why this pattern is true, arguing each of the meters has 100 centimeters, so 3 meters will have 300 centimeters and more generally explaining the smaller the unit the more of unit there will be when measuring the same object (MP.3).

*Disclaimer: Success Criteria is the evidence students must produce to demonstrate learning. These examples are not comprehensive. (Sample Optional Unit 2 Assessment)

Practice Standards and Number Sense Resources:	
Mathematics Practice Standards, Games and Routines	<u>1st Semester Take-Home Games -TheresaWills Games</u>
(Introduced in the first week and used throughout the	-EnVisionMathGamesInvestigations Math Words and
year) Math Practices & Problem Solving Handbook	Ideas -Investigations Math Games -Family Math Games
Problem Solving Organizer The Problem with Key Words	<u>5th grade Home Letters</u>
Numberless Word Problem Example Three Reads	- <u>5th grade additional practice</u> Word Wall Cards
<u>Strategy</u>	<u>1st Semester Teaching Tools</u>

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5th grade number sense routines slides (VA) (use number routines 5-10 minutes daily all year in addition to math class time)Math Routines & Resources Sample Daily Math Routines Additional: Number Routines used 5-10 minutes daily all year (MD) 51 Esti-Mysteries Splat	5 th grade Math FCPS Google Site of Resources 5 th grade decimal and fraction anchor charts
Anchor Resources by enVision Topic	Supplemental Resources by Standard
enVision Topic 3 – Fluently Multiply by Multi-digit Whole Numbers 5.NBT.2 5.NBT.5 Possibly omit lesson 3-7 (May need to review 4.NBT.5 & 4.NBT.6 multi-digit multiplication)	5.NBT.2 Multiplying a Whole Number by a Power of 10 5.NBT.5 How to teach Whole Numbers with Base 10 blocks Make the Largest Product (3 x 2-digit) Juice Box Mix-Up Marta's Multiplication Error Multiplying Decimals by 10
enVision Topic 11 – Convert Measurements (Metric only in this unit) 5.MD.1 only teach Metric lessons: 11-4 to 11-6 (approximately two weeks)	Elmer's Multiplication ErrorThe Value of EducationArea Model MultiplicationStarting a Business PBLReview: Graham Fletchers Conceptual Multiplication Cards
Use Hands-On or <u>Online Manipulatives</u> : Base-10 blocks, Place Value Chips , Base-10 sheets Teaching Tool 4- 5, Place Value charts TT3 5th grade anchor charts -Topic 3 Review What You Know Prerequisite Skills -Topic 3 Vocabulary Cards ** <u>Multi-Digit Multiplication Strategies Card Sort - Number &</u> Operations Base Ten ** <u>Egg Spangled Banner 3 Act Task</u> <u>Desmos four-function calculator</u>	Bucky the Badger 3 Act Math Task The Factor Game online The Product Game online Multi Digit Multiplication Concept Card Sort slides Review: Factors and Multiples Number Puzzles - Operations & Algebraic Thinking One Grain of Rice Literature Link 5.MD.1 Compare Metric Units **Measurement Card Sort - Metric Comparisons and Conversions
enVision Topic 4 – Use Models and Strategies to Multiply Decimals 5.NBT.2 5.NBT.7 Possibly omit lesson 4-7 & 4-10	 5th grade decimal and fraction anchor charts 5.NBT.2 Multiplying a Decimal by a Power of 10 5.NBT.7 How to teach Decimals with Base 10 blocks

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(approximately three weeks) Hands-On or Online Manipulatives: Base-10 blocks, Base-10 sheets Teaching Tool 4-5, Decimal Grids TT7- 9 Topic 4 Review What You Know Prerequisite Skills Desmos four-function calculator **Granny Smith's Skins 3 Act Math Task **Sugar Cubes 3 Act Math Task	Multiplying Tenths on a Grid Digital Activity Multiplying Decimals FAL Game Area Model Decimals - Multiplication Decimals Area Model - PhET Interactive Simulations (colorado.edu) Multiplying Decimals (Decimal x Decimal) Straighten Up 3 Act Math Task Coin Spiral 3 Act Math Task GA Multiplying and Dividing Decimals
enVision Topic 5 - Use Models and Strategies to Divide Whole Numbers 5.NBT.6 Possibly omit lesson 5-6 & 5-8, Teach Calculator strategies (approximately two weeks) Hands-On or Online Manipulatives: Base-10 blocks, Base-10 sheets Teaching Tool 4-5, Grid Paper TT9&10 Topic 5 Review What You Know Prerequisite Skills Desmos four-function calculator	5.NBT.6 How to teach Whole Numbers with Base 10 blocks Division and Interpreting Remainders FAL - Number & Operations in Base Ten Division Strategy: Multiplying Up Water Relief Estimate the Quotient Minutes and Days Dividing with Remainders Formative Assessment Lesson The Multiply/Divide Range Game
enVision Topic 6 – Use Models and Strategies to Divide Decimals 5.NBT.2 5.NBT.7 Possibly combine lessons 6-1 & 6-2 and 6-5 & 6-6 take 2 days for lesson 6-7, Possibly omit 6-9, Teach Calculator strategies (approximately two weeks) Hands-On or Online Manipulatives: Base-10 blocks &	5.NBT.2 5.NBT.7 Lesson6-4Reteach Lesson6-6CenterGames Dividing Decimals with Base Ten Blocks Modeling Decimal Division with Base Ten Blocks (digital) The Value of Education What is 23 ÷ 5? Multiplication and Division with Decimals Game - Number & Operations in Base Ten Hanging By a Hair Granny 3 Act Math Task

Grade: 5

FCPS 2023 - 2024 Math Unit 2 Framework

Unit 2 Multiplying and Dividing Whole Numbers and Decimals, Convert in Metric

Teaching Tool Base-10 sheets 4-5, Place Value chart TT6, Decimal Grids TT7-8, Grid Paper TT9&10, Focus on	<u>Towers of Coins 3 Act Math Task</u> <u>Kendall Hunt Illustrative math decimals unit</u>	
calculator understanding	GA Multiplying and Dividing Decimals	
Topic 6 Review What You Know Prerequisite Skills		
**Decimal Maze (use with calculator)		
Tomato-Tomato 3 Act Math Task		
Desmos four-function calculator		
Summative Assessment		
(Common Unit Assessment on ADAM) This unit assessment will focus on conceptual models of multiplication and division		

(Common Unit Assessment on ADAM) This unit assessment will focus on conceptual models of multiplication and division of whole numbers and decimals using properties with various representations to solve problems......